

# High-Pressure Phase Equilibrium and Raman Spectroscopic Studies on the Nitrous Oxide Hydrate System

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Thermodynamic stability boundaries of nitrous oxide (N<sub>2</sub>O) hydrate and Raman spectra of the N<sub>2</sub>O and host water molecules in the N<sub>2</sub>O hydrate system were investigated in a temperature range of (275.20 to 298.19) K and a pressure range up to 305 MPa. Two three-phase coexisting curves of (hydrate + aqueous + gas) and (hydrate + aqueous + liquid N<sub>2</sub>O) originate from the quadruple point of (hydrate + aqueous + liquid N<sub>2</sub>O + gas) located at (285.15 ± 0.05) K and (4.2 ± 0.1) MPa. The phase behavior of the N<sub>2</sub>O hydrate system is similar to that of the carbon dioxide (CO<sub>2</sub>) hydrate system up to 100 MPa, while the stability boundaries of the N<sub>2</sub>O hydrate system are shifted parallel to the (2 to 3) K higher temperature side than that of CO<sub>2</sub> hydrate. Raman peak splitting of the intramolecular vibration mode for the nitrous oxide molecule in the hydrate phase indicates the occupancy of the nitrous oxide molecule in both small and large cages of structure-I, and this observation is also corroborated by the pressure-induced Raman shift of the lattice mode.

## Introduction

Gas hydrates are crystalline substances composed of the guest species and the cages which are constructed by the hydrogen-bonded water molecules. For about 200 years since the presence of gas hydrates was reported for the first time, many investigators have clarified the structure and thermodynamic stability boundary of gas hydrates with more than 120 guest species. Three common structures of gas hydrate are called structure-I (s-I), structure-II, and structure-H.<sup>1</sup> The s-I hydrate has two small cages (pentagonal dodecahedron, S-cages) and six middle cages (tetrakaidecahedron, M-cages) in the unit lattice. The familiar guest species for s-I are methane (CH<sub>4</sub>, 0.44 nm), carbon dioxide (CO<sub>2</sub>, 0.50 nm), ethane (C<sub>2</sub>H<sub>6</sub>, 0.53 nm), ethylene (C<sub>2</sub>H<sub>4</sub>, 0.55 nm) and so on. The value in parentheses represents the largest van der Waals diameter of each guest species. The Raman peak corresponding to the intramolecular C–H symmetric vibration mode of the CH<sub>4</sub> molecule in the CH<sub>4</sub> hydrate divides into doublets, and the peak intensity ratio corresponds to the cage-constituent ratio of s-I.<sup>2,3</sup> The C<sub>2</sub>H<sub>4</sub> and C<sub>2</sub>H<sub>6</sub> molecules, which are slightly larger than the void space of the S-cage, can oppressively occupy a part of the S-cage as the pressure increases, while they cannot occupy it in a low-pressure region.<sup>4,5</sup>

Nitrous oxide (N<sub>2</sub>O, 0.51 nm) is one of the guest species forming a s-I hydrate. N<sub>2</sub>O hydrate has a long history, and the existence of the N<sub>2</sub>O hydrate was found by Villard in 1888.<sup>6</sup> After that, the thermodynamic stability boundary was reported in a lower-pressure region than the quadruple point (Q<sub>2</sub>) of (hydrate + aqueous + liquid N<sub>2</sub>O + gas).<sup>7,8</sup> Recently, Mohammadi and Richon<sup>9</sup> reported the phase relations of N<sub>2</sub>O hydrate accompanied with CO<sub>2</sub> hydrate. N<sub>2</sub>O has a similar molecular mass and similar critical constants to CO<sub>2</sub>. The largest van der Waals diameter of N<sub>2</sub>O (0.51 nm) is slightly larger than

that of CO<sub>2</sub> (0.50 nm), and it is almost the same as the void size of the S-cage of s-I. In the CO<sub>2</sub> hydrate system, it had been believed that the CO<sub>2</sub> molecule cannot occupy the S-cage. However, the occupancy of CO<sub>2</sub> in both S- and M-cages is confirmed by the single-crystal X-ray diffraction<sup>10</sup> and FTIR<sup>11</sup> measurements. Therefore, it is very important to investigate the S-cage occupancy of N<sub>2</sub>O as well as the phase equilibrium relation of the N<sub>2</sub>O hydrate system.

In the present study, we have investigated the thermodynamic stability boundaries of the N<sub>2</sub>O hydrate system in a temperature range of (275.20 to 298.19) K and a pressure range up to 305 MPa. In addition, the S-cage occupancy of the N<sub>2</sub>O molecule and the pressure effect of the lattice mode of the N<sub>2</sub>O hydrate have been briefly discussed from the Raman spectra of the intra- and intermolecular vibration modes.

## Experimental Section

Research grade N<sub>2</sub>O (purity is higher than 99.9 %) was purchased from Neriki Gas Co. Ltd. The distilled water was obtained from Yashima Pure Chemicals Co. Ltd. Both were used without further purification.

We used three types of high-pressure cells depending on the experimental pressures. The detail of the high-pressure cells is given elsewhere.<sup>12</sup> The equilibrium temperature was measured within a reproducibility of 0.02 K using a thermistor probe (Takara D-641) calibrated by a Pt resistance thermometer (25 Ω) defined by ITS-90. For pressure measurement, two different pressure gauges were used depending on the experimental pressure. Up to 75 MPa, a pressure gauge (Valcom VPRT) calibrated by a Ruska quartz Bourdon tube gauge was used with an estimated maximum uncertainty of 0.02 MPa. Over 75 MPa, a pressure transducer (NMB STD-5000K) and digital peak holder (NMB CSD-819) were used with an estimated maximum uncertainty of 2 MPa.

A desired amount of N<sub>2</sub>O was introduced into the evacuated and cooled cell. A mixing magnet or a mixing ball in the cell

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**Table 1. Thermodynamic Stability Boundaries (Temperature  $T$ , Pressure  $p$ ) of (Hydrate + Aqueous + Gas) and (Hydrate + Aqueous + Liquid  $N_2O$ ) in the  $N_2O$  Hydrate System**

$T/K$	$p/MPa$	$T/K$	$p/MPa$
hydrate + aqueous + gas		hydrate + aqueous + liquid $N_2O$	
275.20	1.20	285.80	10.56
276.25	1.32	286.34	16.12
277.01	1.45	286.35	16.25
277.71	1.58	286.43	17.01
278.39	1.70	286.51	17.75
279.18	1.87	286.74	20.36
279.94	2.04	287.03	23.58
280.73	2.26	287.30	26.72
281.51	2.48	287.35	27.31
282.39	2.79	287.45	28.28
282.79	2.94	287.60	30.21
283.19	3.12	288.03	35.35
283.47	3.24	288.38	39.57
283.67	3.34	288.79	44.89
283.87	3.41	289.11	49.21
284.06	3.54	289.31	52.38
284.37	3.76	289.52	55.43
284.58	3.91	289.71	58.10
284.76	3.99	289.98	61.67
284.97	4.15	291.85	91
		292.83	107
		296.26	202
		298.19	305

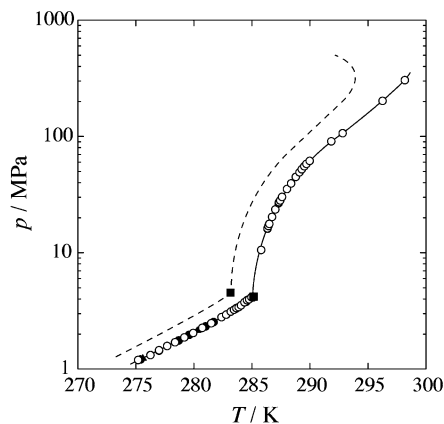
was vibrated from the outside for agitation. The contents were pressurized up to the desired pressure by a successive supply of water. After the formation of the  $N_2O$  hydrate, to establish the three-phase equilibrium state, the system temperature was gradually increased, and the contents were agitated intermittently. The phase behavior of the system was observed by the CCD camera through the sapphire window. To avoid a hysteresis effect, the stability boundary was measured with an annealing method.<sup>13</sup>

After the single crystal of  $N_2O$  hydrate was prepared on the stability boundary under a few pressure conditions,  $N_2O$  hydrate crystals were analyzed using a laser Raman microprobe spectrometer with a multichannel CCD detector (Jobin Yvon Ramanor T64000). The laser beam from the object lens irradiated the sample through the upper sapphire window. The backscatter of the opposite direction was taken in with the same lens. The argon ion laser beam of 514.5 nm and 100 mW was condensed to a 2  $\mu\text{m}$  spot diameter. The spectral resolution was 0.7  $\text{cm}^{-1}$ .

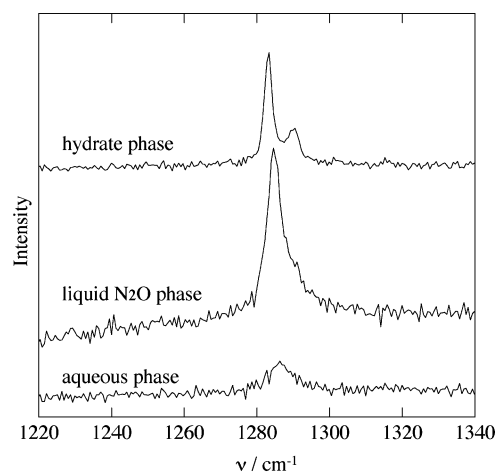
## Results and Discussion

The thermodynamic stability boundaries of  $N_2O$  hydrate are listed in Table 1 and plotted in Figure 1. It is also compared with that of  $CO_2$  hydrate.<sup>12,14</sup> The quadruple point  $Q_2$  of (hydrate + aqueous + liquid  $N_2O$  + gas) phases, which was determined by the extrapolation of two three-phase coexistence curves, is located at  $(285.15 \pm 0.05)$  K and  $(4.2 \pm 0.1)$  MPa. The stability boundary in the lower-pressure range than the  $Q_2$  agrees well with the literature.<sup>6-9</sup> The equilibrium temperature of  $N_2O$  hydrate is (2 to 3) K higher than that of  $CO_2$  hydrate at the same pressure conditions below 100 MPa. Above 100 MPa, the temperature difference becomes gradually large, and it is 4.5 K at around 300 MPa.

From the slope of the equilibrium curve ( $dp/dT$ ) in a lower-pressure region than  $Q_2$ , the overall enthalpy of hydrate dissociation ( $\Delta_{\text{hyd}}H$ ) in the  $N_2O$  hydrate system was obtained by using the Clapeyron equation, the Soave-Redlich-Kwong equation of state,<sup>15</sup> and the ideal hydrate assumption of s-I. The details are given in the previous paper.<sup>16</sup> The average value of



**Figure 1.** Thermodynamic phase boundaries of  $N_2O$  (open circles, present study; closed triangles, ref 7; closed circles, ref 9) and  $CO_2$  (broken lines, refs 12 and 14) hydrate systems. The closed square symbols stand for the quadruple point  $Q_2$  of hydrate + gas + liquid guest + aqueous phases.



**Figure 2.** In situ Raman spectra corresponding to the N-O vibration mode of the  $N_2O$  molecule in  $N_2O$  hydrate and liquid  $N_2O$  and aqueous phases at 40 MPa and 288.43 K.

$\Delta_{\text{hyd}}H = (65 \pm 4)$   $\text{kJ}\cdot\text{mol}^{-1}$  shows good agreement with the literature value of 61.5  $\text{kJ}\cdot\text{mol}^{-1}$ .<sup>17</sup>

The  $N_2O$  molecule has three Raman-active vibration modes, N-O stretching vibration (around 1285  $\text{cm}^{-1}$ ), N-N stretching vibration (around 2230  $\text{cm}^{-1}$ ), and N-N-O bending vibration (around 580  $\text{cm}^{-1}$ ). The Raman peak of the N-O stretching vibration mode is the most intensive of the three Raman-active modes. Figure 2 shows the typical in situ Raman spectra corresponding to N-O vibration of the  $N_2O$  molecule in the hydrate, liquid  $N_2O$ , and aqueous phases on the thermodynamic stability boundary at 40 MPa and 288.43 K. The spectrum splits into a doublet (1283  $\text{cm}^{-1}$  and 1290  $\text{cm}^{-1}$ ) in the  $N_2O$  hydrate phase, while a single peak is detected in both the liquid  $N_2O$  (1285  $\text{cm}^{-1}$ ) and aqueous (1287  $\text{cm}^{-1}$ ) phases. The shoulder at the higher wavenumber side of the Raman peak in the liquid  $N_2O$  phase is the overlap of the peak in the aqueous phase because small  $N_2O$  droplets are dispersed in the aqueous phase. The split of the Raman peak in the hydrate phase indicates that the  $N_2O$  molecules occupy both the S- and M-cages. The stronger peak (1283  $\text{cm}^{-1}$ ) corresponds to  $N_2O$  entrapped in the M-cages and the weaker one (1290  $\text{cm}^{-1}$ ) to the S-cages. This is also supported by the peak intensity ratio of  $N_2O$  in M-cage to S-cage, which is close to the cage-constituent ratio of the s-I hydrate. The Raman spectrum in the hydrate phase reveals that, even at 40 MPa, most of the S-cages are occupied by the  $N_2O$  molecules.

The Raman spectrum corresponding to the intermolecular O—O vibration (lattice mode) between water molecules depends on the hydrate structures, the pressure, and temperature conditions. On the thermodynamic stability boundary of hydrates, the pressure dependences of the O—O vibration energy are peculiar to the hydrate crystal structures for the s-I and s-II.<sup>12,13,18–21</sup> There are two types of pressure dependences in the s-I hydrate systems. One is strong pressure dependence (CH<sub>4</sub>,<sup>3</sup> CO<sub>2</sub>,<sup>12</sup> Xe,<sup>19</sup> and so on, type A). The other is very weak pressure dependence (ethane,<sup>5</sup> cyclopropane,<sup>20</sup> CF<sub>4</sub>,<sup>21</sup> and so on, type B). The Raman peak of the O—O vibration in the N<sub>2</sub>O hydrate crystal (not shown) is located at  $(204 \pm 2) \text{ cm}^{-1}$  (40 MPa and 288.23 K) and  $(210 \pm 2) \text{ cm}^{-1}$  (203 MPa and 296.39 K). The larger deviation than the original accuracy of the Raman spectrometer is caused by the low signal-to-noise ratio because it is more difficult than other hydrate systems to prepare a single crystal of N<sub>2</sub>O hydrate along the thermodynamic stability boundary. Nevertheless, we can barely distinguish the pressure effect of the Raman shift. The pressure dependence of the O—O vibration energy in the N<sub>2</sub>O hydrate is similar to that in the CO<sub>2</sub> hydrate system; that is, it belongs to the type A group of s-I. The stronger pressure dependence would indicate a higher shrinkage of the hydrogen-bonded cage or the larger free volume for the N<sub>2</sub>O molecule.

## Conclusion

We measured the thermodynamic stability boundaries of the N<sub>2</sub>O hydrate system in a pressure range up to 305 MPa. The phase behavior of the N<sub>2</sub>O hydrate system is qualitatively similar to that of the CO<sub>2</sub> hydrate system up to 100 MPa. One of the most important findings is that N<sub>2</sub>O molecules can easily occupy both S- and M-cages of the structure-I hydrate. The peak intensity ratio of N<sub>2</sub>O in the S-cage to the M-cage at 40 MPa and 288.15 K is close to the cage-constituent ratio of structure-I.

## Acknowledgment

The authors are grateful to the Division of Chemical Engineering, Graduate School of Engineering Science, Osaka University, for the scientific support by “Gas-Hydrate Analyzing System (GHAS)”.

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Received for review March 31, 2009. Accepted April 30, 2009.

JE900318U